



Functional programming in Erlang

Lecture 6 of TDA384/DIT391
Principles of Concurrent Programming

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Based on course slides by Carlo A. Furia and Sandro Stucki

Today's menu

What is Erlang?

Types

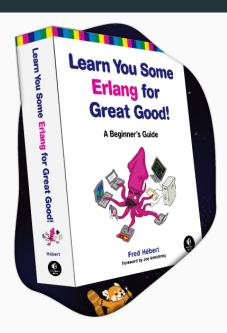
Expressions and patterns

Function definitions

Recursion

Impure and higher-order functions

Don't forget...



What is Erlang?

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Erlang combines a functional language with message-passing features:

- The <u>functional part</u> is <u>sequential</u>, and is used to define the behavior of <u>processes</u>.
- The <u>message-passing</u> part is highly <u>concurrent</u>: it implements the <u>actor model</u>, where actors are Erlang processes.

This class covers the functional/sequential part of Erlang.

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rent computation

1985 Agha further refines the actor

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Late 1980s Erlang's implementation becomes

efficient; Erlang code is used in

production at Ericsson

1998 Ericsson bans Erlang, which be-

comes open-source

Late 2000s Erlang and the actor model make

a come-back in mainstream pro-

gramming



Erlang in the real world

Erlang has made a significant impact in the practice of concurrent programming by making the formal actor model applicable to real-world scenarios.

Initially, Erlang was mainly used for telecommuncation software:

- Ericsson's AXD301 switch includes over one million lines of Erlang code; achieves "nine 9s" availability (99.9999999%)
- cellular communication infrastructure (services such as SMSs)

Recently, it has been rediscovered for Internet communication apps:

- WhatsApp's communication services are written in Erlang
- Facebook Chat (in the past)

Why Erlang?

We've faced many challenges in meeting the evergrowing demand for [the WhatsApp] messaging services, but [...] Erlang continues to prove its capability as a versatile, reliable, high-performance platform.

Rick Reed, 2014 -

That's 'Billion' with a 'B': Scaling to the next level at WhatsApp

The language itself has many pros and cons, but we chose Erlang to power [Facebook] Chat because its model lends itself well to concurrent, distributed, and robust programming.

Chris Piro, 2010 – Chat Stability and Scalability

What is a functional language?

Functional languages are based on elements quite different from those imperative languages are based on.

Imperative languages – such as Java – are based on:

- state variables
- state modifications assignments
- · iteration loops

Functional languages – such as Erlang – are based on:

- data values
- functions on data without side effects
- functional forms function composition, higher-order functions

What is a functional language?

Functional languages are based on elements quite different from those imperative languages are based on.

```
Imperative languages – such as Java – are based on:
```

An imperative program is a sequence of state modifications on variables.

```
// compute X<sup>n</sup>
int power(int x, int n) {
  int result = 1;
  for (int i = n; i < n; i++)
    result *= x;
  return result;
}</pre>
```

Functional languages – such as Erlang – are based on:

A functional program is the side-effect-free application of functions on values.

```
% compute X^N
power(X, 0) -> 1;
power(X, N) -> X * power(X, N-1).
```

In functional programs, variables store immutable values, which can be copied but not modified.

The Erlang shell

You can experiment with Erlang using its shell, which can evaluate expressions on the fly without need to define complete programs.

Notice you have to terminate all expressions with a period. Functions are normally defined in external files, and then used in the shell. Compilation targets bytecode by default.

Types

Types, dynamically

A type constrains:

- 1. The (kinds) of values that an expression can take
- 2. The functions that can be applied to expressions of that type

For example, the integer type:

- 1. includes integer values (1, -100, 234, ...), but not, say, decimal numbers (10.3, -4.3311, ...) or strings ("hello!", "why not", ...)
- 2. supports functions such as sum +, but not, say, logical and

Erlang is dynamically typed:

- programs do not use type declarations
- the type of an expression is only determined at runtime, when the expression is evaluated
- if there is a type mismatch (for example 3 + false) expression evaluation fails

Erlang types include primitive and compound data types.

An overview of Erlang types

Erlang offers eight primitive types:

- Integers: arbitrary-size integers with the usual operations
- · Atoms: roughly corresponding to identifiers
- Floats: 64-bit floating point numbers
- · References: globally unique symbols
- · Binaries: sequences of bytes
- Pids: process identifiers
- · Ports: for communication
- Funs: function closures

And three + two compound types (a.k.a. type constructors):

- Tuples: fixed-size containers
- Lists: dynamically-sized containers
- Maps: key-value associative tables (a.k.a. dictionaries) recent feature, experimental in Erlang/OTP R17
- Strings: syntactic sugar for sequences of characters
- · Records: syntactic sugar to access tuple elements by name

Numbers

Numeric types include integers and floats. We will mainly use integers, which are arbitrary-size, and thus do not overflow.

EXPRESSION	VALUE	
3	3	explicit constant ("term")
1 + 3	4	addition
1 - 3	-2	subtraction
4 * 2	8	multiplication
5 div 4	1	integer division
5 rem 3	2	integer remainder
5 / 4	1.25	float division
power(10,1000)	100000000	no overflow!
2#101	5	101 in base 2
16#A1	161	A1 in base 16

Atoms

Atoms are used to denote distinguished values; they are similar to symbolic uninterpreted constants. An atom can be:

- a sequence of alphanumeric characters and underscores, starting with a <u>lowercase</u> letter, <u>or</u>
- an arbitrary sequence of characters (including spaces and escape sequences) between single quotes

Examples of valid atoms:

```
x
a_Longer_Atom
'Uppercase_Ok_in_quotes'
'This is crazy!'
true
```

Booleans

In Erlang there is no Boolean type; instead, the atoms true and false are conventionally used to represent Boolean values.

MEANING
egation
onjunction (evaluates both arguments/eager)
isjunction (evaluates both arguments/eager)
xclusive or (evaluates both arguments/eager)
onjunction (short-circuited/lazy)
isjunction (short-circuited/lazy)

Examples:

```
true or (10 + false) % error: type mismatch in second argument
true orelse (10 + false) % true: only evaluates first argument
```

Relational operators

Erlang's relational operators have a few syntactic differences with those of most other programming languages.

OPERATOR	MEANING
<	less than
>	greater than
=<	less than or equal to
>=	greater than or equal to
=:=	equal to
=/=	not equal to
==	numeric equal to
/=	numeric not equal to

Examples:

```
3 =:= 3 % true: same value, same type
3 =:= 3.0 % false: same value, different type
3 == 3.0 % true: same value, type not checked
```

Order between different types

Erlang defines an order relationship between values of any type. When different types are compared, the following order applies:

```
number < atom < reference < fun < port < pid < tuple < map < list
```

Thus, the following inequalities hold:

When comparing lists to lists and tuples to tuples:

- · comparison is by size first;
- two lists or two tuples with the same size are compared <u>element</u> by element, and satisfy the comparison only if all pairs satisfy it.

Tuples

Tuples denote ordered sequences with a fixed (but arbitrary for each tuple instance) number of elements. They are written as comma-separated sequences enclosed in curly braces. Examples of valid tuples:

```
{ } % empty tuple
{ 10, 12, 98 }
{ 8.88, false, aToM } % elements may have different types
{ 10, { -1, true } } % tuples can be nested
```

Functions on a tuple T:

FI	п	N	\cap	ГΙ	10	J.

RETURNED VALUE

```
element(N, T) Nth element of T

setelement(N, T, X) a copy of T, with the Nth element replaced by X

tuple_size(T) number of elements in T

element(2, {a, b, c}) % b: tuples are numbered from 1

setelement(1, {a, b}, z) % {z, b}

tuple_size({ }) % 0
```

Lists

Lists denote ordered sequences with a variable (but immutable for any list instance) number of elements. They are written as comma-separated lists enclosed in square brackets.

Examples of valid lists:

List operators

Some useful functions on lists L:

FUNCTION	RETURNED VALUE
length(L)	number of elements in L
[H L]	a copy of L with н added as first ("head") element
hd(L)	L's first element (the "head")
tl(L)	a copy of L without the first element (the "tail")
L1 ++ L2	the concatenation of lists L1 and L2
L1 L2	a copy of L1 with all elements in L2 removed
	(with repetitions, and in the order they appear in L1)

Operator | is also called cons; using it, we can define any list:

```
[1, 2, 3, 4] =:= [1 | [2 | [3 | [4 | []]]]]
hd([H | T]) =:= H
tl([H | T]) =:= T
% this is an example of --
[1, 2, 3, 4, 2] -- [1, 5, 2] =:= [3, 4]
```

Strings

Strings are sequences of characters enclosed between double quotation marks. Strings are just syntactic sugar for <u>lists of character</u> codes.

String concatenation is implicit whenever multiple strings are juxtaposed without any operators in the middle.

Using strings (\$c denotes the integer code of character c):

```
"" % empty string =:= empty list
"hello!"
"hello" "world" % =:= "helloworld"
"xyz" =:= [$x, $y, $z] =:= [120, 121, 122] % true
[97, 98, 99] % evaluates to "abc"!
```

Records

Records are ordered sequences with a fixed number of elements, where each element has an atom as name. Records are just syntactic sugar for tuples where positions are named.

```
% define 'person' record type
  % with two fields: 'name' with default value "add name"
  %
                       'age' without default value (undefined)
-record(person, { name="add name", age })
  % 'person' record value with given name and age
#person{name="Joe", age=55}
#person{age=35, name="Jane"} % fields can be given in any order
  % when a field is not initialized, the default applies
#person{age=22} =:= #person{name="add name", age=22}
  % evaluates to 'age' of 'Student' (of record type 'person')
Student#person.age
```

Erlang's shell does <u>not know</u> about records, which can only be used in modules. In the shell, #person{age=7, name="x"} is {person, "x", 7}.

Expressions and patterns

Variables

Variables are identifiers that can be bound to values; they are similar to constants in an imperative programming language. A variable name is a sequence of alphanumeric characters, underscores, and @, starting with an <u>uppercase</u> letter or an underscore.

In the shell, you can directly bind values to variable:

- Evaluating Var = expr binds the value of expression expr to variable Var, and returns such value as value of the whole binding expression
- · Each variable can only be bound once
- To clear the binding of variable Var evaluate f(Var)
- Evaluating f() clears all variable bindings
- The anonymous variable _ ("any") is used like a variable whose value can be ignored

In modules, variables are used with <u>pattern matching</u>, which we present later.

Expressions and evaluation

Expressions are evaluated exhaustively to a value – sometimes called (ground) term: a number, an atom, a list, ...

The order of evaluation is given by the usual precedence rules; using parentheses forces the evaluation order to be inside-out of the nesting structure.

Some precedence rules to be aware of:

- · and has higher precedence than or
- · andalso has higher precedence than orelse
- when lazy (andalso, orelse) and eager (and, or) Boolean operators are mixed, they all have the same precedence and are left-associative
- ++ and -- are right-associative
- relational operators have lower precedence than Boolean operators; thus you have to use parentheses in expressions such as (3 > 0) and (2 == 2.0)

Precedence rules: examples

3 + 2 * 4	% is 11
3 + (2 * 4)	% is 11
(3 + 2) * 4	% is 20
true or false and false	% is true
true orelse false andalso false	% is true
true or false andalso false	% is false
true orelse false and false	% is true (why?)

Patterns

Pattern matching is a flexible and concise mechanism to bind values to variables. It is widely used in functional programming languages to define functions on data (especially lists); Erlang is no exception.

A pattern has the same structure as a term, but in a pattern some parts of the term may be replaced by free variables.

Examples of patterns:

```
3
A
{X, Y}
{X, 3}
[H | T]
[H | [21]
```

Note that a pattern may contain <u>bound</u> variables; in this case, evaluating the pattern implicitly evaluates its bound variables.

Pattern matching

Pattern matching is the process that, given a pattern P and a term T, binds the variables in P to match the values in T according to P and T's structure. If P's structure (or type) cannot match T's, pattern matching fails.

PATTERN	I = TERM	BINDINGS
3	= 3	none
Α	= 3	A: 3
Α	= B	if B is bound then A =:= B; otherwise fail
{X,Y}	= 3	fail (structure mismatch)
{X,Y}	= {1, 2}	X: 1, Y: 2
{X,Y}	= {"a",[2,3]}	X: "a", Y: [2,3]
[H T]	= [1,2]	H: 1, T: [2]
[H [2]]	= [1,2]	H: 1
[F,S]	= [foo,bar]	F: foo, S: bar
{X,Y}	= [1,2]	fail (type mismatch)

Pattern matching: notation

Given a pattern P and a term T, we write $\langle P \triangleq T \rangle$ to denote the pattern match of T to P. If the match is successful, it determines bindings of the variables in P to terms. Given an expression E, we write

$$\mathsf{E}\langle\mathsf{P}\triangleq\mathsf{T}\rangle$$

to denote the term obtained by applying the bindings of the pattern match $\langle P \triangleq T \rangle$ to the variables in E with the same names. If the pattern match fails, $E\langle P \triangleq T \rangle$ is undefined.

Examples:

- $(X + Y)(\{X, Y\} \triangleq \{3, 2\})$ is 5
- (T ++ [2]) \langle [H|T] \triangleq [8] \rangle is [2]
- $H\langle [H|T] \triangleq [] \rangle$ is undefined

The notation $E\langle P \triangleq T \rangle$ is not valid Erlang, but we use it to illustrate Erlang's semantics.

Multiple expressions

Multiple expressions E1, ..., En can be combined in a compound expression obtained by separating them using commas. Evaluating the compound expression entails evaluating all component expressions in the order they appear, and returning the value of the last component expression as the value of the whole compound expression. A single failing evaluation makes the whole compound expression evaluation fail.

Multiple expression blocks

Using blocks delimited by begin...end, we can introduce multiple expressions where commas would normally be interpreted in a different way.

This may be useful in function calls:

```
power(2, begin X=3, 4*X end) % returns power(2, 12)
```

Without **begin...end**, the expression would be interpreted as calling a function power with three arguments.

List comprehensions

List comprehensions provide a convenient syntax to define lists using pattern matching.

A list comprehension is an expression of the form

```
[ Expression || P1 <- L1, ..., Pm <-Ln, C1, ..., Cn ]
```

where each Pk is a <u>pattern</u>, each Lk is a <u>list expression</u>, and each Ck is a <u>condition</u> (a Boolean expression). Intuitively, each pattern Pk is matched to every element of Lk, thus determining a binding B; if substituting all bound values makes all conditions evaluate to true, the value obtained by substituting all bound values in Expression is accumulated in the list result; otherwise the binding is ignored.

Modules

A module is a collection of function definitions grouped in a file. Indeed, modules are the only places where functions can be defined – they cannot directly be defined in the shell. The main elements of a module are as follows:

Compiling and using a module in the shell:

```
1> c(foo). % compile module 'foo' in current directory
{ok,foo}. % compilation successful
2> foo:up_to_5(). % call 'up_to_5' in module 'foo'
[1,2,3,4,5]
```

Function definitions

Function definitions: basics

In Erlang, like every functional programming language, functions are the fundamental units of computation. A function defines how to map values to other values; unlike in imperative programming languages, most functions in Erlang have no side effects: they do not change the state of the program executing them (especially their arguments).

The basic definition of an n-argument function f (arity n), denoted by f/n, has the form:

$$\overbrace{f(P1,\ldots,Pn)}^{\text{head}} \xrightarrow{\text{body}}$$

- The function name f is an atom
- The function's formal arguments P1, ..., Pn are patterns
- The body E is an <u>expression</u> normally including variables that appear in the arguments

```
identity(X) -> X. % the identity function sum(X, Y) -> X + Y. % the sum function
```

Examples of function definitions

The most fundamental definition of an n-argument function f (arity n), denoted by f/n, has the form:

Some examples:

Function call/evaluation

Given the definition of a function f/n:

$$f(P1, \ldots, Pn) \rightarrow E.$$

a call expression to f/n has the form:

and is evaluated as follows:

- 1. for each $1 \le k \le n$, evaluate Ak, which gives a term Tk
- 2. for each $1 \le k \le n$, pattern match Tk to Pk
- 3. if all pattern matches are successful, the call expression evaluates to $E\langle P1,\ldots,Pn\triangleq T1,\ldots,Tn\rangle$
- 4. otherwise, the evaluation of the call expression fails

Examples of function calls

DEFINITIONS	CALLS	VALUE
zero() -> 0. identity(X) -> X.	zero() identity({1,2,3})	0 {1,2,3}
<pre>sum(X, Y) -> X + Y. head([H _]) -> H. tail([_ T]) -> T.</pre>	<pre>sum(zero(), second({2,3})) head([]) head([3,4,5])</pre>	fail
second({_, Y}) -> Y. positives(L) ->	tail([]) positives([-2,3,-1,6,0])	fail
$[X \mid X < L, X > 0].$	positives([2,3, 1,0,0])	[3,0]

Function definition: clauses

Function definitions can include multiple clauses, separated by semicolons:

A call expression is evaluated against each clause in textual order; the first successful match is returned as the result of the call.

Therefore, we should enumerate clauses from more to less specific.

```
lazy_or(true, _) -> true;
lazy_or(_, true) -> true;
lazy_or(_, _) -> false.
```

this function does not work as expected unless this clause is listed last

Pattern matching with records

Pattern matching an expression R of record type rec

$$rec{f1=P1, ..., fn=Pn} = R$$

succeeds if, for all $1 \le k \le n$, field fk in R's evaluation — that is, R#name.fk — matches to pattern Pk. If record type rec has fields other than $f1, \ldots, fn$, they are ignored in the match.

Thanks to this behavior, using arguments of record type provides a simple way to extend data definitions without having to change the signature of all functions that use that datatype.

Flexible arguments with records: example

```
-record(error, {code}).
error_message(#error{code=100}) -> io.format("Wrong address");
error_message(#error{code=101}) -> io.format("Invalid username");
    ...
error_message(_) -> io.format("Unknown error").
```

If we want to add more information to the type error, we only have to change the record definition, and the clauses using the new information:

Compare this to the case where we would have had to change error_message from a unary to a binary function!

Function definition: guards

Clauses in function definitions can include any number of guards (also called conditions):

```
f(Pk1,..., Pkn) when Ck1, Ck2,... -> Ek;
```

A guarded clause is selected only if all guards Ck1, Ck2,... evaluate to true under the match, that is if $Cki\langle Pk1,...,Pkn \triangleq Tk1,...,Tkn \rangle$ evaluates to true for all guards Cki in the clause.

More generally, two guards can be separated by either a comma or a semicolon: commas behave like lazy and (both guards have to hold); semicolon behave like lazy or (at least one guard has to hold).

Type checking – at runtime

Since Erlang is dynamically typed, there are cases where we have to test the actual type of an expression – for example, because a certain operation is only applicable to values of a certain type.

To this end, Erlang provides several test functions whose names are self-explanatory:

```
is_atom/1
is_boolean/1
is_float/1
is_integer/1
is_list/1
is_number/1
is_pid/1
is_port/1
is_tuple/1
```

Use these only when necessary: in most cases defining implicitly partial functions is enough.

Function definition: local binding

The expression body in a function definition can include compound expressions with bindings:

```
f(Pk1,..., Pkn) -> V1=E1,..., Vw=Ew, Ek;
```

Such bindings are only visible within the function definition.

They are useful to define shorthands in the definition of complex expressions.

```
volume({cylinder, Radius, Height}) ->
  Pi=3.1415,
  BaseArea=Pi*Radius*Radius,
  Volume=BaseArea*Height,
  Volume.
```

If expressions (guard patterns)

Ifs provide a way to express conditions alternative to guards (in fact, ifs are called – somewhat confusingly – guard patterns in Erlang). An if expression:

```
if
    C1 -> E1;
    :
    Cm -> Em
end
```

evaluates to the expression Ek of the first guard Ck in textual order that evaluates to true; if no guard evaluates to true, evaluating the **if** expression fails.

```
age(Age) ->
if Age > 21 -> adult;
   Age > 11 -> adolescent;
   Age > 2 -> child;
   true -> baby end.
```

Case expressions

Cases provide an additional way to use pattern matching to define expressions. A case expression:

```
case E of
P1 -> E1;
:
Pm -> Em
end
```

evaluates to $Ek\langle Pk \triangleq T \rangle$, where E evaluates to T, and Pk is the first pattern in textual order that T matches to; if T matches no pattern, evaluating the case expression fails. Patterns may include when clauses, with the same meaning as in function definitions.

Which one should I use?

Having several different ways of defining a function can be confusing. There are no absolute rules, but here are some guidelines that help you write idiomatic code:

- the first option to try is using pattern matching directly in a function's arguments, using different clauses for different cases
- if parts of a pattern expression depend on others, you may consider using case expressions to have nested patterns
- you do not need if expressions very often (but it's good to know what they mean, and sometimes they may be appropriate)

Recursion

Recursion in programming

Recursion is a style of programming where functions are defined in terms of themselves.

The definition of a function f is recursive if it includes a call to f (directly or indirectly).

Recursion in mathematics

Recursion is a style of definition where concepts are defined in terms of themselves.

The definition of a concept is recursive if it defines the concept in terms of an instance of the concept itself.

Definition of natural numbers:

- 0 is a natural number;
- if n is a natural number then n+1 is a natural number.



Recursion in programming provides a natural way of implementing recursive definitions in mathematics.

$$n! \triangleq \underbrace{n \cdot (n-1) \cdot \cdots \cdot 1}_{n \text{ terms}}$$

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$$n! \triangleq \begin{cases} 1 & \text{if } 0 \leq n \leq 1 \leftarrow \text{ base case} \\ n \cdot (n-1)! & \text{if } n > 1 \leftarrow \text{ recursive/inductive case} \end{cases}$$

Recursion in programming provides a natural way of implementing recursive definitions in mathematics.

$$n! \triangleq \begin{cases} 1 & \text{if } 0 \le n \le 1 \leftarrow \text{base case} \\ n \cdot (n-1)! & \text{if } n > 1 \leftarrow \text{recursive/inductive case} \end{cases}$$

- Each recursive call triggers an independent evaluation of the recursive function. (Independent means that it works on its own private copy of actual argument expressions.)
- When a recursive instance terminates evaluation, its value is used in the calling instance for its own evaluation.

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eval 

3 * factorial(2)
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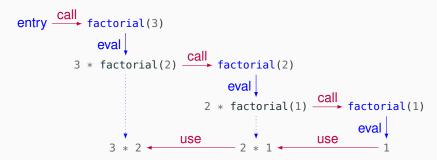
eval 

2 * factorial(1) factorial(1)
```

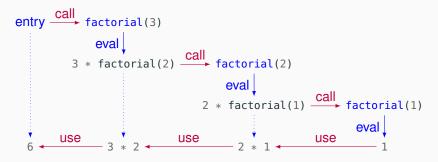
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Recursion as a design technique

Recursion as a programming technique is useful to design programs using the divide and conquer approach:

To solve a problem instance P, split P into problem instances P_1, \ldots, P_n chosen such that:

- 1. Solving P_1, \ldots, P_n is simpler than solving P directly
- 2. The solution to P is a simple combination of the solutions to P_1, \ldots, P_n

In functional programming, recursion goes hand in hand with pattern matching:

- pattern matching splits a function argument's into smaller bits according to the input's structure
- recursive function definitions define the base cases directly, and combine simpler cases into more complex ones

Recursive functions: sum of list

Define a function sum(L) that returns the sum of all numbers in L.

- 1. The base case (the simplest possible) is when L is empty: $sum([1]) \rightarrow 0$
- 2. Let now L be non-empty: a non empty list matches the pattern [H|T]
 - H is a single number, which we must add to the result
 - T is a list, which we can sum by calling sum recursively

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```
sum([]) -> 0; % base case sum([H|T]) -> H + sum(T). % recursive case
```

can we switch the order of clauses?

To make the function more robust, we can skip over all non-numeric elements:

Recursive functions: last list element

Define a function last(L) that returns the last element of L.

- 1. When L is empty, last is undefined, so we can ignore this case
- 2. The simplest case is then when L is one element: last([E]) -> E
- Let now L be non-empty: a non empty list matches the pattern [H|T]
 - · E is the first element, which we throw away
 - T is a list, whose last element we get by calling last recursively

```
last([E]) -> E; % base case
last([_|T]) -> last(T). % recursive case
```

Can T match the empty list?

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```
last([E]) -> E; % base case
last([_|T]) -> last(T). % recursive case
```

Can T match the empty list? No, because neither of the clauses match the empty list. To make this explicit, we could write:

```
last([E|[]])-> E; % base case
last([_|T]) -> last(T). % recursive case
```

Tail recursion

A recursive function f is tail recursive if the evaluation of f's body evaluates the recursive call last.

Tail-recursive functions are generally <u>more efficient</u> than general-recursive functions. When efficiency is <u>not an issue</u>, there is no need to use a tail-recursive style; but we will use tail-recursive functions extensively (and naturally) when implementing servers.

Tail recursion

A recursive function f is tail recursive if the evaluation of f's body evaluates the recursive call last.

overloading: two functions power/2 and power/3

```
% general recursive:
power(_, 0) ->
1;
power(X, N) ->
X * power(X, N-1).
% tail recursive:
power(X, N) ->
power(X, N, 1).
power(X, N, 1).
Accumulator;
power(X, N, Accumulator) ->
power(X, N-1, X*Accumulator).
```

Tail-recursive functions are generally <u>more efficient</u> than general-recursive functions. When efficiency is <u>not an issue</u>, there is no need to use a tail-recursive style; but we will use tail-recursive functions extensively (and naturally) when implementing servers.

Impure and higher-order

functions

Where are all the statements, assignments, loops?

Statements, assignments, and loops are not available as such in Erlang. Everything is an expression that gets evaluated.

- (side-effect free) expressions are used instead of statements
- (pure) functions return modified copies of their arguments instead of modifying the arguments themselves
- one-time bindings are used instead of assignments that change values to variables
- · recursion is used instead of loops

The sparse presence of side effects helps make functional programs higher level than imperative ones.

Printing to screen

line 2

The expressions we have used so far have no side effects, that is they do not change the state but simply evaluate to a value. Not all expressions are side-effect free in Erlang. Input/output is an obvious exception: to print something to screen, we evaluate an expression call, whose side effect is printing.

% print the string Format, interpreting control sequences on Data
io:format(Format, Data)

CONTROL SEQUENCE	DATA
~B	integer
~g	float
~\$	string
~p	any Erlang term
~n	line break

```
1> io:format("~s ~B. ~p~n~s ~B~n", ["line", 1, true, "line", 2]). line 1. true
```

Exception handling

Erlang has an exception handling mechanism that is similar to a functional version of Java's try/catch/finally blocks.

```
try Expr of
   Success1 -> Expr1;
   ...
catch
   Error1:Fail1 -> Recov1;
   ...
after After end
```

- The try blocks behaves like a case block
- If evaluating Expr raises an exception, it gets pattern matched against the clauses in catch (Errork's are error types, Failk's are patterns, and Recovk's are expressions)
- Expression After in the after clause always gets evaluated in the end (but does not return any value: used to close resources)

Exception handling: example

Function safe_plus tries to evaluate the sum of its arguments; if evaluation succeeds, it returns the result; if evaluation raises a badarith exception, it returns false.

```
safe_plus(X, Y) ->
  try X + Y of
    N -> N
  catch
    error:badarith -> false
end.
```

Example of using it:

```
1> safe_plus(2, 3).
5
2> safe_plus(2, []).
false
```

Functions are values too

Functions are first-class objects in Erlang: they can be <u>passed</u>
<u>around</u> like any other values, and they can be <u>arguments</u> of functions.

A function f/k defined in module m is passed as argument fun m: f/k.

This makes it easy to define functions that apply other functions to values following a pattern.

```
% apply function F to all elements in list L
map(F, []) -> [];
map(F, [H|T]) -> [F(H)|map(F,T)].

1> map(fun m:age/1, [12, 1, 30, 56]). % we defined age before
[adolescent,baby,adult,adult]
```

A function that takes another function as argument is called higher-order.

Inline functions

Sometimes it is necessary to define a function directly in an expression where it is used. For this we can use anonymous functions – also called <u>lambdas</u>, <u>closures</u>, or <u>funs</u> (the last is Erlang jargon):

```
fun
  (A1) -> E1;
     :
     (An) -> En
end
```

where each Ak is a sequence of patterns, and each Ek is a body.

```
% double every number in the list
1> map(fun (X)->2*X end, [12, 1, 30, 56]).
[24,2,50,112]
```

Working on lists

Module lists includes many useful predefined functions to work on lists. These are some you should know about – but check out the full module documentation at http://erlang.org/doc/man/lists.html.

```
all(Pred, List) % do all elements E of List satisfy Pred(E)?
any(Pred, List) % does any element E of List satisfy Pred(E)?
filter(Pred, List) % all elements E of List that satisfy Pred(E)
last(List) % last element of List
map(Fun, List) % apply Fun to all elements of List
member(Elem, List) % is Elem an element of List?
reverse(List) % List in reverse order
seq(From, To) % list [From, From+1, ..., To]
seq(From, To, I) % list [From, From+I, ..., ~To]
```

Folds

Several functions compute their result by recursively accumulating values from a list:

```
sum([]) -> 0; len([]) -> 0; sum([H|T]) -> H + sum(T). len([H|T]) -> 1 + len(T).
```

We can generalize this pattern into a single higher-order function fold(F, R, L): starting from an initial value R, combine all elements of list L using function F and accumulate the result.

```
fold(_-, Result, []) -> Result; fold(F, Result, [H|T]) -> F(H, fold(F, Result, T)).
```

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```
fold(_-, Result, []) -> Result;

fold(F, Result, [H|T]) -> F(H, fold(F, Result, T)).
```

Using fold, we can define sum and len:

```
 \begin{split} & sum(L) \  \, -> & len(L) \  \, -> \\ & fold(\textbf{fun} \ (X,Y) -> X+Y \ \textbf{end}, \ \theta, \ L) \, . & fold(\textbf{fun} \ (X,Y) -> 1+Y \ \textbf{end}, \ \theta, \ L) \, . \end{split}
```

Erlang module lists offers functions foldr/3 (which behaves like our fold) and foldl/3 (a tail-recursive version of fold, with the same arguments).

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